2018

CBCS

3rd Semester

MATHEMATICS

PAPER-C7T

(Honours)

Full Marks: 40

Time: 2 Hours

The figures in the right-hand margin indicate full marks.

Candidates are required to give their answers in their own words as far as practicable.

| Illustrate the answers wherever necessary.
| [Calculator is allowed in examination Hall]

### Numerical Methods

# the standard of UNIT-I

1. Answer any two questions :

 $2 \times 2$ 

(a) If a number 0.05418 is approximated to 0.05411, find the number of significant digits for such approximation.

- (b) Define the terms :
  - (i) Truncation error
  - (ii) Round of error
- (c) Let,  $u = 4x^6 + 3x 9$ . Find the percentage error in computing u at x = 1.1, if the error in x is 0.05.

#### UNIT-II

2. Answer any one question :

1×2

- (a) Write down the equation  $x^3 + 2x 10 = 0$  in the form  $x = \varphi(x)$  such that the iterative scheme about x = 2 converges.
- (b) What do you mean by the term as iterative method has the rate of convergence  $p(\ge 1)$ ?
- 3. Answer any one question :

1×5

(a) Find the iterative formula for finding  $\sqrt[K]{N}$ , where N is a real number, using Newton-Raphson formula. Hence evaluate  $\sqrt[3]{2}$  correct upto four significant figure. State the condition of convergence of this method.

(b) Describe the method of false position for finding a real root of an equation f(x) = 0 and obtain the corresponding interation formula. Discuss its advantages and disadvantages in comparison to Newton-Raphson Method.

#### UNIT-III

4. Answer any one question :

1×2

- (a) State the conditions for convergence of Gauss-Scidel method for solving a system of linear equations. Are they necessary and sufficient?
- (b) Define ill-conditioned and well-conditioned system of Linear equation.
- 5. Answer any one question :

1×5

(a) Consider a system of equations

$$x + y - z = 2$$

$$2x + 3y + 5z = -3$$

$$3x + 2y - 3z = 6$$

Solve the system of equations by LU decompositon method.

(b) Describe Gauss elimination method with pivoting for solution of a system of linear equation, what is the total number of operations required for this method?

#### UNIT-IV

6. Answer any one question :

1×10

(a) (i) Prove that 
$$f(x+Kh) = \sum_{i=0}^{K} (K_{C_i}) \Delta^i f(x)$$

(ii) Find the missing term of the following table :

x	0	1	2	3	4	5
f(x)	0	_	8	15	11_1-	35

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(iii) Obtain the Error in the Lagrange Interpolating Polynomia.

Also show that the maximum error in linear interpolation is given by  $\frac{(x_0 - x_1)^2}{8}M$  where  $M = \max |f''(\xi)|, x_0 \le \xi \le x_1$ .

(b) What is the *n*th order forward differences of a polynomial of degree n? If n is very small prove that  $\Delta^{n+1} f(x) = h^{n+1} f^{n+1}(x).$ 

Find the value of Sec 31.5° using the following table:

θ (in degree)	31°	32°	33°	34°
tanθ	0.6008	0.6249	0.6494	0.6747

## UNIT-V

7. Answer any one question :

1×2

- (a) Show that Simpson's ½ rule is exact for integrating a polynomial of degree 3.
- (b) If f(x) is a quadratic polynomial, deduce that  $\int_{1}^{3} f(x)dx \approx \frac{1}{12}[f(0) + 22f(2) + f(4)]$
- 8. Answer any one question :

1×5

(a) Derive Simpson's one-third Rule from Newton cotes formula.

(b) Describe the method of least squares to fit a straight line y = ax + b.

In some determinations of the value v of carbon dioxide dissolved in a given volume of water at different temparature  $\theta$ , the following pairs of values were obtained:

θ	0	5	10	15
υ	1.80	1.45	1.18	1.00

Obtain by the method of least square a relation of the form  $v = a + b\theta$  which best fit to this observat

# UNIT-VI

9. Answer any one question :

1×5

(a) Describe Euler's method for solving first order differential equation with initial condition. Compute y(1.2) for the problem  $\frac{dy}{dx} = 1 + xy$ , y(1) = 1 by modified Euler's method taking h = 0.1.

(b) Find the values of y(0.1) and y(0.2) using Runge Kutta Method of 4th order taking h = 0.1. Given that  $\frac{dy}{dx} = xy + y^2, \ y(0) = 1.$ 

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